## Simulation of (tropical) forest stands using marked point processes

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### **Description of a forest stand**



List of trees (x<sub>i</sub>, y<sub>i</sub>, D<sub>i</sub>, s<sub>i</sub>)
spatial coordinates (x, y)
diameter D (height...)
species s

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### Spatialized information is required, e.g.

To run an individual-based space-dependent model of forest dynamics initial state for management-oriented simulations To make simulation study of such a model repetitions To make simulation study of distance-based estimators of wood biomass, etc.

### ... but is rarely available



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### Disaggregation

#### How to simulate a virtual forest stand given partial data?

$$\left.\begin{array}{c} (D_i, s_i)\\ N, f(D), f(s)\\ N, \bar{D}, f(s) \end{array}\right\} \to (x_i, y_i, D_i, s_i)$$

→ Fit a model (point process) to a reference forest stand with parameters that can be estimated from partial data

### High species diversity

Hundreds of species/ha in tropical moist forest About 40 species/ha in tropical dry forest Simplification: grey species (otherwise: see Goreaud, 2004; Loussier, 2003)

→ Marked point process (mark = diameter)

### Fitting to a reference forest stand

T In terms of spatial pattern: intensity, second-order characteristics (pair correlation function, Ripley's K-function)



**P** In terms of diameter distribution

T Interaction between diameter and spatial pattern

### **Computing time constraint**

Simulation of a virtual has to be fast

(compared to the time required by an individual-based space-dependent model to reach stationary state)

## **Spatial pattern**

- homogeneity and isotropy is assumed
- intensity
- Ripley's *K*-function

### **Diameter distribution**

- histogram of diameters
- variogram (as if it was a random field)

## Interaction between diameter and spatial pattern

- Schlather (2001); Parrott & Lange (2004):
- 1. mark variogram?
- 2. Cressie's mark covariance function?
- 3. Stoyan's mark covariance function?
- 4. Stoyan's mark correlation function  $(k_{mm})$ ?

- 5. Isham's mark correlation function?
- 6. mark difference function?
- 7. mark expectation function?

### Conditional K-function given $D \ge x$

Or: 
$$\frac{\Pr[\|\mathbf{x} - \mathbf{x}'\| \le r | D < D']}{\Pr[\|\mathbf{x} - \mathbf{x}'\| \le r]}$$

### **Random field model**

- $\Psi$ : marked process
- $\Phi$ : unmarked process
- Z: random field

$$\Psi = \bigcup_{x \in \Phi} [x; Z(x)]$$

and 
$$Z$$
 independent of  $\Phi$ .  
Schlather (2002); Schlather  $et \ al.$  (2004): test of

dependence between marks and locations for Gaussian marks

Diameter has exponential distribution

### First case study: Mali savannas





OAcacia macrostachya OCombretum glutinosum OGuiera senegalensis OEntada africana OPteleopsis suberosa

Oautres espèces

## Korokoro, *K*-function (all trees)



## Korokoro, Matérn process



## Korokoro, log Gaussian Cox process



Distance (r)

## Korokoro, Poisson-gamma process



Distance (r)

# Diameter: exponential random field with exponential covariance function

Simulation using tessellation method (Schlather, 1999):



# Korokoro, diameter distribution & variogram



## Korokoro: interaction diameter/positions



Distance (m)

## Random field model (Matérn process)



Distance (m)

### Second case study: Paracou



Since 1984, 120 ha, over 46,000 trees monitored

# **Plot 1 in 1984 (** $D \ge 10$ cm**)**



## Angelique in South block in 1999



## K-function, plot 1 in 1984, $D \ge 10$ cm



## K-function, plot 1 in 1984, $D \ge x$



## Individual-based space-dependent models as space-time marked point processes

Rathbun & Cressie (1994), Stoyan & Penttinen (2000):



## **SELVA model**



## **SELVA** model, *K*-function



# Another model with short-range interactions



## **Stationary state**, *K*-function



## Stationary state, K-function, $D \ge 22$ cm



### Stationary state, diameter distribution



## Observed pattern might be reproduced by a model with

clustered recruitment

short-range competition

... but simulation time very long  $\dot{\bigcirc}$ 



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