

Estimation of species relative abundances and habitat preferences using opportunistic data

Camille Coron ^{*1}, Clément Calenge², Christophe Giraud¹, and Romain Julliard³

¹Laboratoire de Mathématiques d’Orsay, Univ. Paris-Sud, CNRS, Université Paris-Saclay, 91405 Orsay, France.

²Office national de la chasse et de la faune sauvage, Saint Benoist, BP 20. 78612 Le Perray en Yvelines, France.

³CESCO, UMR CNRS 7204, Muséum National d’Histoire Naturelle, 55 rue Buffon, 75005 Paris, France

April 14, 2017

Keywords: Citizen science; opportunistic data; estimation of species relative abundances; habitat selection; resource selection function

Abstract

We develop a new statistical procedure to monitor, with opportunist data, relative species abundances and their respective preferences for different habitat types. Following Giraud et al. (2015), we combine the opportunistic data with some standardized data in order to correct the bias inherent to the opportunistic data collection. Our main contributions are (i) to tackle the bias induced by habitat selection behaviors, (ii) to handle data where the habitat type associated to each observation is unknown, (iii) to estimate probabilities of selection of habitat for the species. As an illustration, we estimate common bird species habitat preferences and abundances in the region of Aquitaine (France).

1 Introduction

Citizen science programs have been increasingly developed for biodiversity monitoring during the last 20 years. These programs usually enroll a large number of volunteers to work on a given scientific issue. For example, breeding bird surveys aim at estimating population trends of bird species in a given area (Link and Sauer (1998)); the bird observations by the volunteers of the program populate a database describing the number of individuals of every focus species observed at a given time and place. Since the observational effort is usually much larger in citizen science programs than in “professional” scientific programs, citizen science programs usually gather much more observations than classical programs.

The issues tackled by citizen science programs can be very diverse, including the estimation of the spatial distribution of a set of species at different spatial scales (Royle et al. (2005);

*camille.coron@math.u-psud.fr, corresponding author

Fithian et al. (2014); Giraud et al. (2015)), the study of certain ecological behaviors such as habitat selection (e.g., Biggs and Olden (2011)), or the monitoring of population trends of endangered species (Link and Sauer (1998)). Although some citizen science programs rely on data collected with standardized protocol and sampling design (e.g. the North American Breeding Bird Survey, Link and Sauer (1998)), many others rely on the opportunistic collection of observations by the volunteers, with an unknown observation intensity. In the following, we will refer to this sort of uncontrolled data collection by “opportunistic data collection”. In this paper, we focus on the estimation of some relative abundances based on such opportunistic data.

The opportunistic nature of these data raises important statistical issues (Dickinson et al. (2010), Isaac et al. (2014)). A major issue is due to the non-uniform observation intensity: the collected data cannot be considered as an unbiased sample of the individuals present on this area. Any statistical approach relying on such data must tackle this data collection bias in some way. Some recent papers (Giraud et al. (2015); Fithian et al. (2014)) proposed to handle this bias by combining this biased opportunistic dataset with a (possibly much smaller) dataset collected in the same area by a more classical program with a known observational effort (hereafter called “standardized dataset”). Under some restrictive assumptions (discussed below), such a combination provides some unbiased estimates of the relative abundance for the species monitored in at least one of the two programs. An attractive feature of these estimation schemes is to provide relative abundance estimation for species monitored in the opportunistic dataset, but not in the standardized dataset. This allows, in principle, to monitor with opportunistic data collection some rare species that would be much more costly to monitor with a classical standardized program.

The approach proposed in Giraud et al. (2015) provides, for a set of species, some relative abundance estimates in a collection of sites. The statistical modeling accounts for unequal and unknown detectability and reporting rates for the monitored species, both in the opportunistic and the standardized dataset, and for the unequal and unknown observational intensity in the opportunistic dataset. Yet, a crucial hypothesis is that the animals are distributed uniformly within each site. When a site gathers several areas with different habitat, and if the proportions of these different habitats differ among sites, this assumption is likely to be violated due to habitat selection behavior. Similarly the observational effort in opportunistic data is not equally distributed across the different habitat types due to observer preference for some habitats (Tulloch and Szabo (2012)). This lack of homogeneity induces some important bias in the estimation, as shown in Bellamy et al. (1998); Mason and Macdonald (2004); Fuller et al. (2005); Fithian et al. (2014). For example, if the volunteers participating to a bird monitoring program are mostly interested in waterbirds, they will strongly select for humid habitat within each site. If humid habitat is rare yet present within a site, most of the observations in this site will be performed in this rare habitat, and the resulting waterbird abundance in this site will be strongly overestimated.

The aim of our paper is to extend the approach of Giraud et al. (2015) by handling (unknown) habitat preferences that might influence both observers and observed animal behaviors. The whole monitored area is described by several habitat categories for which both observers and animals have different preferences. The habitat type associated to each observation is not assumed to be known exactly (e.g. the exact location of the observation is only known approximately, or an observed species observation may not be attributed unambiguously to a surrounding habitat). It can be seen as a hidden variable. Preferences of the observers and of each species for each habitat types are also unknown. Our approach provides estimation for all

of them. Hence, by taking the habitat stratification into account, we produce (i) some more accurate relative abundance estimates; in particular, for given site, it allows to decompose a species relative abundance in a habitat-specific component (e.g., forest birds are relatively more abundant because forests are over-represented in that site) and an additive site-specific component, (ii) relative abundance maps at a finer spatial scale, and (iii) some estimates of the resource selection functions of the species (Manly et al. (2002)), which has major implications for biological conservation. To sum-up, our main contributions are:

- To incorporate habitat type preferences in the statistical modeling of Giraud et al. (2015);
- To handle data where the habitat type associated to each observation is unknown (which allows to gather data at different spatial scale);
- To estimate the relative probabilities of selection of habitat for the monitored species.

We develop our statistical modeling in Section 2. In this new model, the respective habitat selection behaviors of observers and animals are modeled using hidden variables. The spatial distribution of observers in the sites, as well as the habitat selection within the sites is modeled differently for the two datasets (opportunistic and standardized). On the other hand, animals are assumed to distribute within a site according to their preferences for different habitat types. Then, we illustrate our approach using simulated data to demonstrate that it recovers the parameters of the model that was used to simulate the data. Finally, using a real dataset collected on birds in the Aquitaine region (France), we assess the performance of the model for estimating species relative abundances as well as their habitat selection parameters.

2 Model and parameters

In this section, we introduce our statistical modeling of available data. These data are the outcome of some ecological features (species abundances) and some observational bias (detectability, partial reporting, heterogeneous observational effort, etc). Both the ecological features and the observational bias are affected by some ecological variables (for example habitat type, population and/or road density, altitude, as presented in Mair and Ruete (2016)), which will be called habitats, from now on. Our modeling takes into account this double source of bias induced by the habitat. We first describe the ecological ingredients, which are independent from the considered datasets, and then the observational ingredients which are dataset dependent.

Species abundances and habitat selection probability The space-time is divided into units, we call henceforth *sites*, which correspond to the scale at which we will predict the relative abundances. So, each site refers to the couple of a spatial domain and a time interval. We index the sites by $j \in \llbracket 1, J \rrbracket$. The species we focus on, are indexed by $i \in \llbracket 1, I \rrbracket$, and we denote by N_{ij} the number of individuals of species i in the site j . Our aim is to estimate the relative abundances N_{ij}/N_{i1} for all i and j .

The habitat types of a given site j are not homogeneous. Each site j gathers several spatial domains, each with a specific habitat type. We index by $h \in \llbracket 1, H \rrbracket$ the habitat types. The species i are not uniformly distributed in the spatial domain of j : The species i prefer some habitat types to some others and hence are more or less frequent in the different habitat types.

In order to avoid biases in our estimation, we must take this heterogeneity into account. Our modeling assumes that the fraction of the animals of the species i present in the habitat type h inside the site j is proportional to the *known* area V_{hj} of the habitat type h inside the site j weighted by a number $S_{ih} \in [0, 1]$ which represents the preference toward the habitat type h for the species i . More precisely, we assume that the density of the species i at location x in the site j is given by

$$\frac{N_{ij}S_{ih(x)}}{\sum_{h'} S_{ih'}V_{h'j}},$$

with $h(x)$ the habitat type at location x . Following the concept definitions clarified in Lele et al. (2013), the parameters S_{ih} can be interpreted as the probability of selection of habitat h by species i . These probabilities of selection of habitat are *unknown* and we will estimate them.

Observations and reporting As in Giraud et al. (2015), our relative abundance estimation is based on two datasets : (i) a standardized dataset, labeled by $k = 0$, collected under a program with a known sampling effort and (ii) an opportunistic dataset, labeled by $k = 1$, characterized by a completely unknown sampling effort. The datasets gather counts of animals for all sites j . We emphasize that each site j must be surveyed by both datasets, and each species i must be surveyed by at least one of the two datasets (at least one species must be surveyed in both datasets).

We assume that we have informations about the locations of the observations at a finer scale than the site j . Each site j is divided into several (possibly many) cells indexed by c and for each observation, we have the information in which cell c the observation occurred. We emphasize that the cell paving can completely differ between the two datasets. In each dataset, only a (possibly very small) fraction of the cells have been visited at least once by the observers, so we do not have counts for all cells c , but only for a (possibly very small) fraction of them. For a cell c visited in the dataset k , we denote by X_{ick} the corresponding count for the species i . This count X_{ick} is not homogeneously proportional to the abundance of the species i in c . Actually, the counts are biased by the inhomogeneous observational effort (total amount of observation time, number of observers, number or density of traps, etc) and the unequal probability of reporting of the species i (varying detectability, partial reporting, etc). Following Giraud et al. (2015), we denote by \mathcal{E}_{ck} the observation intensity (or effort) in the cell c for the dataset k , and by P_{ik} the probability of detection/reporting of the species i in the dataset k . When the species i are not monitored in the dataset k , the probability of detection/reporting P_{ik} is set to 0. The model of Giraud et al. (2015) does not take into account habitat types and reads $X_{ick} \sim \mathcal{Poisson}(N_{ij}\mathcal{E}_{ck}P_{ik})$. For the sake of comparison with the models described below, we scale the effort \mathcal{E}_{ck} by the area V_j of the site j by introducing $E_{ck} = \mathcal{E}_{ck}V_j$. In terms of this scaled effort, the model of Giraud et al. (2015) is

$$X_{ick} \sim \mathcal{Poisson}(N_{ij}E_{ck}P_{ik}/V_j). \tag{1}$$

Within a cell c , the observers do not scan the space uniformly. Actually, they have some preferences for some habitat types (which are not the same for the two datasets). These preferences induce some specific biases, which must be properly addressed. Similarly as for the probability of selection of habitat, the preference of the observers of the dataset k for the habitat h is represented by a real number $q_{hk} \in [0, 1]$. For the dataset k , we model the

observation intensity at location x within the cell c by

$$\frac{q_{h(x)k} E_{ck}}{\sum_{h'} q_{h'k} V_{h'c}},$$

where V_{hc} is the known area of cell c covered by habitat h . Writing \mathcal{A}_c for the spatial domain of the cell c and taking into account both the probabilities of selection of habitat and the observers habitat preferences, we obtain the modeling for the count of the species i in the cell c for the dataset k

$$\begin{aligned} X_{ick} &\sim \text{Poisson} \left(\int_{\mathcal{A}_c} N_{ij} \frac{S_{ih(x)}}{\sum_{h'} S_{ih'} V_{h'j}} \times E_{ck} \frac{q_{h(x)k}}{\sum_{h'} q_{h'k} V_{h'c}} \times P_{ik} dx \right) \\ &= \text{Poisson} \left(N_{ij} E_{ck} P_{ik} \sum_h \frac{q_{hk}}{\sum_{h'} q_{h'k} V_{h'c}} \times \frac{S_{ih}}{\sum_{h'} S_{ih'} V_{h'j}} V_{hc} \right). \end{aligned} \quad (2)$$

In the above model, recall that the volumes V_{hj} and V_{hc} are known. For the standardized dataset, the observation intensities E_{c0} are assumed to be known (up to a common multiplicative constant), and we assume that (i) either the habitat type associated to each observation X_{jc0} is known, (ii) or the ratios q_{h0}/q_{10} are known for all h (generally equal to 1). All the other parameters are unknown. Their identifiability and the implementation of model (2) are detailed in Appendix A.2.

We point out that, here, we do not take into account a dependence of the detectability with habitat types (due notably to different levels of visibility in different types of habitat). We refer to Section A.5.2 for an extension of this model, integrating a dependence of detection probability with habitat types.

Note finally that when neglecting differences in habitat selection probabilities both for observers and observed individuals, the total number X_{ick} of observations of individuals of species i in cell c of domain j for the dataset k follows the model (1) issued from Giraud et al. (2015).

3 Numerical result

We test our modeling framework both with some simulated data and with some real data. The likelihood of (2) cannot be maximized easily, so we opt for a non-informative bayesian estimation computed with the Gibbs Sampler *JAGS* (Plummer (2003)). This program is called within *R* (R Core Team (2014)) using the *rjags* package (Plummer (2014)). We choose uninformative priors for the unknown parameters and the sampler *JAGS* provides samples distributed according to the posterior distributions for these parameters. The details about the implementation of the estimation procedures are given in Appendix A.2.

3.1 Illustration with simulated data

We illustrate the ability of our estimation procedure to recover the actual parameter values with some simulated datasets. We compare the results of our procedure to those computed according to the model of Giraud et al. (2015), in order to check whether the gain in model specification counterbalances favorably the inflation of the number of parameters.

We simulate two datasets according to the Model (2): A standardized one ($k = 0$) with known relative effort intensities E_{j0}/E_{10} and an opportunistic one ($k = 1$) with unknown relative

effort intensities. For this simulated dataset we consider 20 different species on 30 different sites that are covered by 2 types of habitat. For standardized (resp. opportunistic) data, 10 (resp. 30) cells are visited in each site. The other parameters, such as species abundances, detection probabilities, habitat selection probabilities, or efforts in the opportunistic dataset are sampled according to uniform distributions.

In order to illustrate the impact of the habitat modeling and the gain of using opportunistic data, we compare the three following estimation procedures:

- [Opp+Stand with hab] Our model (2) with unknown habitat selection probabilities and using both opportunistic and standardized data, denoted below by [Opp+Stand with hab];
- [Stand only with hab] Our model (2) with unknown habitat selection probabilities and using only standardized data (which corresponds to Equation (2), with $\bar{k} = 0$ only). It is denoted by [Stand only with hab];
- [Opp+Stand no hab] The model (1) which neglects differences in selection probabilities, using both opportunistic and standardized data. This model is denoted by [Opp+Stand no hab].

In Figure 1, we plot the posterior distributions of relative species abundances obtained for these three models, and the reference relative species abundance values that we estimate are given in red. This figure shows, as proved in Giraud et al. (2015), the improvements brought by opportunistic data, since the estimation obtained by combining the two datasets is both more precise and more accurate. It also illustrates that neglecting habitat preferences can lead to biased estimation of species relative abundances. Figure 5 in Appendix A.4 also gives the posterior distributions of habitat selection probabilities, that give good approximations of the real values given in red. Figure 2 gives the boxplots of the relative differences between the estimated and real relative abundances, for each of the three models. Here, the estimated relative abundances is defined as the mean of the associated posterior distribution, and similar results are obtained using the median of these distributions. Again, we observe that the estimation combining both datasets and taking habitat types into account produces better results; and ignoring habitat types induces a significant bias.

3.2 Real data

3.2.1 Datasets and Habitats

Datasets To investigate whether taking the habitat types into account improves the estimation on real data, we consider the same datasets as in Giraud et al. (2015). These are two different datasets of common birds observations in Aquitaine (south-western French region): standardized data are provided by the French National Hunting and Wildlife Agency (ON-CFS, Office National de la Chasse et de la Faune Sauvage), by the French National Hunters' Association (FNC, Fédération Nationale des Chasseurs) and by the French Departmental Hunters' Associations (FDC, Fédérations Départementales des Chasseurs), while opportunistic data are provided by the French program Faune-Aquitaine, managed by the protection association Ligue pour la Protection des Oiseaux (LPO). Our estimation is assessed using a validation dataset, produced by the French Museum of Natural History.

For the first (standardized) dataset we used the ACT monitoring survey (see Boutin et al. (2003) for more details concerning this dataset and its protocole) in which 13 species of birds

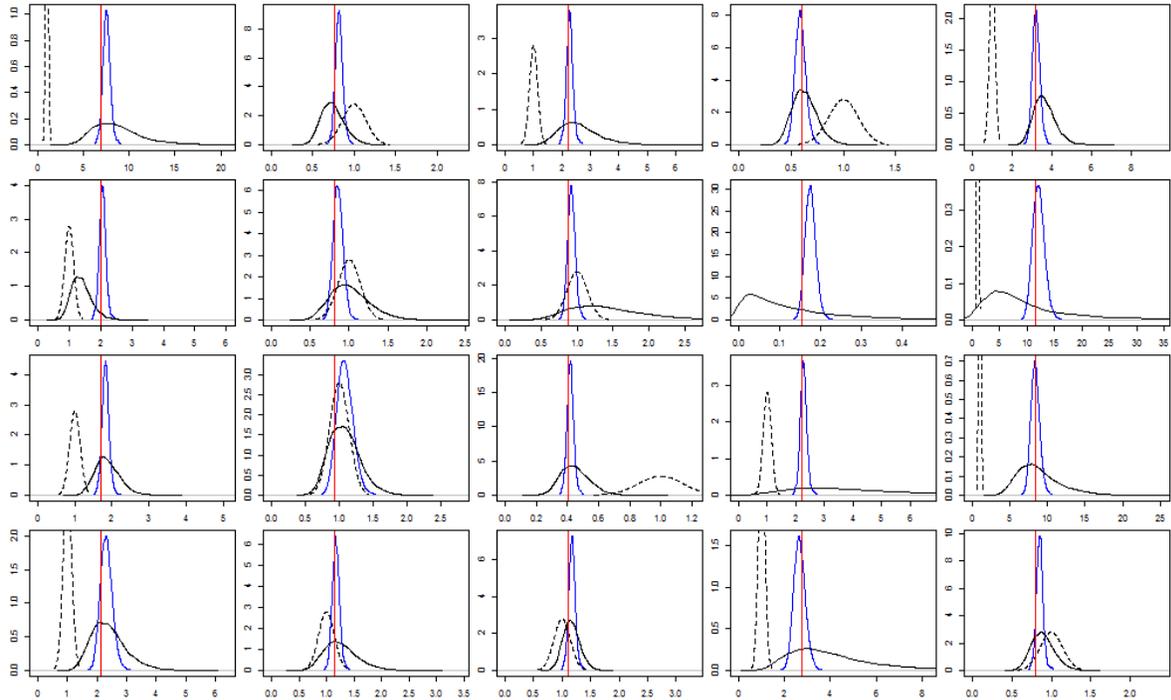


Figure 1: Posterior distributions of the relative abundances N_{i2}/N_{i1} for all i , estimated with [Stand only with hab] (in black), [Opp+Stand with hab] (in blue) and [Opp+Stand no hab] (dotted line). The reference values are given in red.

are monitored (see Table 3). The observers are professionals from the technical staff of the participating organisms. The Aquitaine region was discretized into 66 quadrats, in which a 4-km-long route was randomly placed in non-urban habitat (see Figure 3). Each route was traveled twice between April and mid-June and included 5 points separated by exactly 1 km: at each travel, each point was visited for exactly 10 minutes. The species of every bird heard or seen was recorded, and for each point and each species, we have access to the maximum of the counts from the two visits (in order to take advantage of the maximum detectability and to avoid effects due to migration, as explained in Pollock (1982)). This protocol was repeated for several years and we use data from 2008 to 2011, which finally leads to 239 visits of quadrats (some of the quadrats were not visited each year), therefore leading to $13 * 5 * 239 = 15535$ data, corresponding to the reporting of 7899 birds observations (some species are not always detected).

For opportunistic data, we used the dataset collected by the website www.fauneaquitaine.org (handled by the LPO), on which anyone can register and report the species, number of detected individuals, date, and location associated to any bird observations made in Aquitaine. The level of precision of the location is variable: exact location, locality indication, or commune indication. To deal with this inhomogeneity in location information, for numerical analyses we will use the commune in which was made each observation, which is always given. As previously, we selected all such records between April and mid-June for the years 2008–2011. This led to 693 581 birds observations in 1622 communes (see Figure 3), monitoring 34 species. Note that, to make their observations, observers can go anywhere, for an unknown amount of

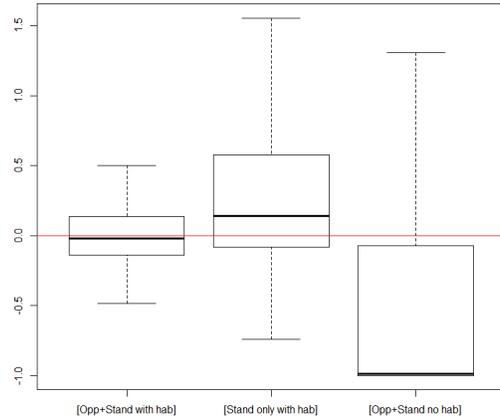


Figure 2: Boxplots of the relative differences $\frac{(\hat{N}_{ij}^{[model]}/\hat{N}_{i1}^{[model]})-(N_{ij}/N_{i1})}{N_{ij}/N_{i1}}$ between the estimated and "real" relative abundances, using data and models [Opp+Stand with hab], [Stand only with hab], and [Opp+Stand no hab].

time, and that they report their observations with an unknown probability (that might depend on the observed species); therefore these data do not provide any information concerning observation effort.

For the validation dataset used to assess the predictive power of our approach, we used the data from the STOC program (*Suivi temporel des oiseaux communs*), which is a French breeding bird survey carried out by the French Museum of Natural History (MNHN, Museum National d'Histoire Naturelle). The protocole of this survey (see Jiguet et al. (2012) for more details) is the following: each observer is assigned a 2×2 km square whose position is uniformly randomly chosen within 10 km of his/her house. The observer then distributes on the considered square, 10 observation points that have to be representative of the different habitats areas on the square, and each point is visited twice between April and mid-June, during 5 minutes. Every observation of each species (hearing or seeing) is reported and the maximum count among the two visits is kept, as for the ACT program. As previously, we use all such records for the years 2008–2011. This leads to 86526 birds observations in 38 squares (see Figure 3), monitoring 34 species (the same than for the LPO dataset).

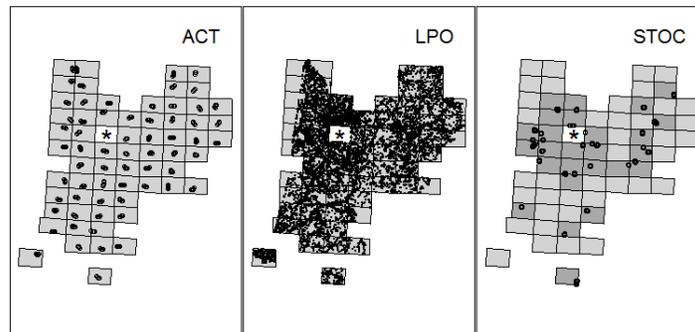


Figure 3: Positions of data collecting

Habitats Land use (habitat) types were based on corine landcover typologies that were grouped in 7 categories in order to reduce complexity and ensure identifiability (see Appendix A.2): urbanized area, intensive agriculture with homogenous landscape (arable land or permanent crop), open natural landscape (natural or pasture), farmland with heterogenous landscape, mixed forest, deciduous forest, and coniferous forest.

3.2.2 Assessing estimation performances

In this section, we compare the estimation performances of the same three statistical models as in the Section 3.1: [Opp+Stand with hab], [Stand only with hab] and [Opp+Stand no hab]. We obtain estimation for the main parameters of interest of the model, namely the relative abundances N_{ij}/N_{i1} for all i, j , and the habitat selection probabilities S_{ih}/S_{i1} for all i, h and q_{h2}/q_{12} for all h . Our goal here is to compare the three estimation schemes, so we do not to discuss the ecological aspects of our estimates. Yet, in Appendix A.5, we provide some abundances maps and some habitat selection probabilities for some species of interest.

To assess the performances of the three models, we investigate their ability to predict the STOC observations X_{ij}^{STOC} , in each quadrat surveyed in the STOC dataset. Since some species (21 among 34, see Appendix A.1 for the exact list) are not surveyed in the ACT dataset, we split apart the results for the species surveyed in ACT and the results for the others. For each species i and each of the three models, we compute a predictor \hat{X}_{ij}^{model} (described in Appendix A.3) of X_{ij}^{STOC} . Then for each species i and each model we compute the Pearson correlation between the vector $(\hat{X}_{ij}^{model})_j$ and the vector $(X_{ij}^{STOC})_j$. The medians (as well as the first and third quartiles) of these correlations (calculated for each species i) are given in Table 1. We notice that the results for the Model (1) slightly differ from the results from Giraud et al. (2015), this can be explained by the fact that we use non-informative Bayesian estimation performed with JAGS instead of maximum likelihood estimation.

| Data and model | Correlations (In ACT) | Correlations (not in ACT) |
|-----------------------|-----------------------|---------------------------|
| [Opp+Stand with hab] | 0.49 (0.30–0.54) | 0.39 (0.12–0.54) |
| [Stand only with hab] | 0.29 (0.03–0.46) | – |
| [Opp+Stand no hab] | 0.44 (0.32–0.68) | 0.31 (0.19–0.42) |

Table 1: Medians of Pearson correlation coefficients (as well as first and third quartiles) between the STOC observations and the estimates of species relative abundances computed with the models [Opp+Stand with hab], [Stand only with hab], and [Opp+Stand no hab].

Figure 4 shows the posterior distributions of the relative abundances $N_{ij}^{[model]}/N_{i1}^{[model]}$ obtained for the three considered situations.

We observe an improvement of the predictions when we take the habitat into account. Actually, when we move from the Model (1) without habitat modeling, to the Model (2) with habitat modeling, the median of the correlations between the vectors $(\hat{X}_{ij}^{model})_j$ and $(X_{ij}^{STOC})_j$ increases from 0.44 to 0.49 for the species surveyed in the standardized dataset (ACT) and from 0.31 to 0.39 for the other species. So, the reduction of the bias obtained by modeling the habitat is stronger than the increase of the variance induced by the inflation of the number of parameters. This feature is confirmed by the difference between the BIC value for the model

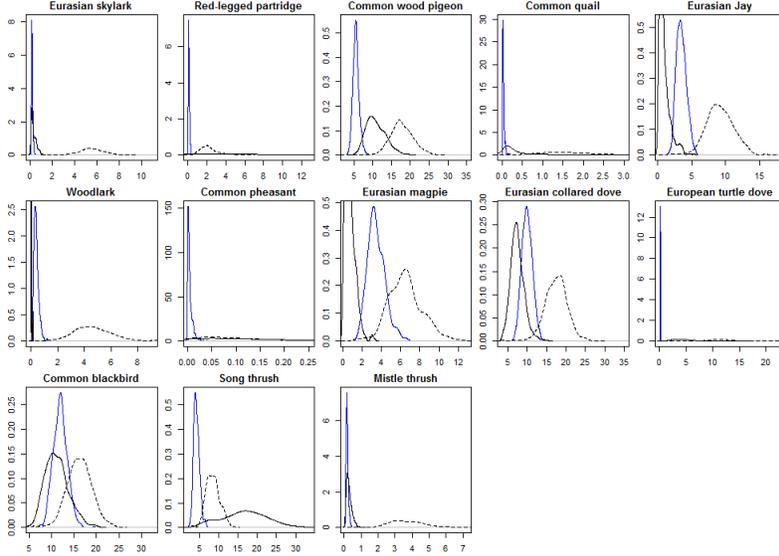


Figure 4: Posterior of the relative abundances $\hat{N}_{ij}^{[model]} / \hat{N}_{i1}^{[model]}$ of species i monitored in the ACT program and $j = 62$, and using data and models [Opp+Stand with hab] (blue), [Stand only with hab] (black), and [Opp+Stand no hab] (dotted line).

[Opp+Stand with hab] and the model [Opp+Stand no hab]:

$$\Delta BIC = BIC(\text{Opp} + \text{Stand with hab}) - BIC(\text{Opp} + \text{Stand no hab}) = -8867.$$

This improvement can be explained by the strong differences in habitat selection parameters S_{ih} that we have estimated (see Figure 7), confirming that habitat biases cannot be ignored. This feature is also supported by the shape of the posterior distribution of the model with habitat [Opp+Stand with hab] which is much more spiked than the shape of the posterior distribution of the model without habitat [Opp+Stand no hab].

In addition, as in Giraud et al. (2015), we observe that adding the opportunist data in our estimation improves the estimation. In particular, we observe that for our dataset, the improvement brought from the use of opportunistic data is stronger than the improvement brought from habitat modeling. In the next paragraph, we investigate the importance of the habitat structure in the spatial variation of abundance.

3.2.3 Models of spatial repartition

In our model (2), we incorporate two sources of abundance variation. Part of the variation in abundance is explained by the habitat structure. This part is driven by the habitat selection probability S_{ih} . The remaining of the abundance variation comes from some other factors, acting differentially on the different sites j . We investigate below whether the spatial repartition of individuals is mainly explained by habitat structure, or if some other factors have a major role. In the first case, most of the variation in the spatial variation would be explained by the variations of the ratio $S_{ih(x)} / (\sum_h S_{ih} V_{hj})$; while in the second case, a major part of the spatial variation would be explained by the variations with j of the N_{ij} . In order to compare the relative importance of both effects, we compare the models derived from (2)

by first neglecting the variation in the habitat selection probabilities S_{ih} (setting them all to 1); second by neglecting the variation in j of the N_{ij} , replacing all of them by a single value N_i . As explained before, when all the habitat selection probabilities S_{ih} are equal, the model (2) reduces to the model (1) of Giraud et al. (2015). So to investigate the relative importance of the habitat types with respect to the other factors, we compare the model [Opp+Stand with hab] and [Opp+Stand no hab] with the [One Quadrat with hab] model where

$$\text{[One Quadrat with hab]} \quad X_{ick} \sim \mathcal{Poisson} \left(N_i E_{ck} P_{ik} \sum_h \frac{q_{hk}}{\sum_{h'} q_{h'k} V_{h'c}} \frac{S_{ih}}{\sum_{h'} S_{ih'} V_{h'}} V_{hc} \right),$$

where V_h is the total area of habitat h in the considered space.

For each model, we compute as previously the Pearson correlations between the observations of the STOC dataset and the estimation of these observations using each of the three models. The median and the quartiles for all the species are given in Table 2.

| Data and model | Correlations |
|------------------------|-------------------|
| [Opp+Stand with hab] | 0.45 (0.23–0.54) |
| [One Quadrat with hab] | 0.15 (-0.03–0.36) |
| [Opp+Stand no hab] | 0.38 (0.26–0.52) |

Table 2: Medians (as well as first and third quartiles) of Pearson correlation coefficients between estimation of species relative abundances using different models of species spatial repartition.

We observe that, in our case, the overall fit for the [one quadrat] model is poorer. This point is confirmed by the BIC values

$$\Delta BIC = BIC([\text{Opp} + \text{Stand no hab}]) - BIC([\text{One Quadrat with hab}]) = -813853.$$

The habitat type therefore does not seem to be the main driver of the spatial variation for most of the considered species on the considered space (though this ecological result can be different when considering other species on an other space, notably with more diverse types of habitats). The study of the impact of habitat structure on the estimates for each species relative abundance is presented in Section 4.

4 Discussion

Main results. We have developed a new statistical approach relying on the joint use of two datasets collected respectively by an opportunistic data collection program and by a classical standardized monitoring program with a known (and ideally controlled) observation intensity. By combining these two datasets, our approach estimates the relative abundance of a set of species in a set of sites, while accounting for the different detectability of the species in the two programs, variable habitat preferences by both the species and the observers, and unknown observation intensity in the opportunistic data collection program. The use of opportunistic data in this approach results in a considerably increased precision in comparison to the estimation that would be based only on the standardized data. Note also that our approach allows the estimation of the relative abundances of some species monitored only with

the opportunistic data collection program, as long as there are at least several other species monitored by the two programs. Our approach extends the statistical modeling developed in Giraud et al. (2015), by taking into account the variable preferences of habitat types by both the species and the observers. We show in the present paper that by accounting for habitat preferences by both the species and the observers in the citizen science program, our approach results in less bias and an increased performance of the relative abundances estimates. This is illustrated by a simulated dataset, as well as a practical case study.

A useful byproduct of this approach is the estimation of the relative preferences of each species for each habitat type: more precisely, the estimated value of the habitat selection parameters S_{ih} corresponds to the relative probability of selection of habitat h , which is exactly the definition of a resource selection function (RSF, Lele et al. (2013)), a tool widely used in biological conservation and wildlife management to identify important habitat for a given species on a study area (Boyce and McDonald (1999)). Existing statistical approaches for the fit of RSF rely on the comparison of an unbiased sample of the habitat used by the focus species, and an unbiased sample of either the unused habitat or the habitat available to the species (see a list of possible statistical approaches in Manly et al. (2002), especially chapter 4 for the case where habitat is defined by several categories). The collection of such data can be expensive, and when the study area is large and/or the focus species is rare it can become prohibitive (see the conclusion of MacKenzie (2005)). However, endangered rare species are precisely those for which information on selected places is the most crucial. The situation is generally worsened when several rare and endangered species are under study. Citizen science programs relying on opportunistic data collection are a very attractive alternative in this context because of the large observation effort carried out, but are often notoriously flawed by an unequal and unknown observation effort, which make their use in such studies difficult (Phillips et al. (2009)). If at least a part of the species monitored in the opportunistic data collection program are also monitored in a more classical standardized program, our approach provides a way to correct for the biases caused by the unequal observation effort in opportunistic data collection programs, and therefore to benefit of the large observation effort for the RSF estimation. Our approach therefore allows the batch estimation of the RSF for all species in the opportunistic data collection program.

Limitations. Our approach relies on the hypothesis that the preferences of a given species for a given habitat type does not vary into space and time. Several authors have shown that this might not always be the case: animals sometimes show a functional response of habitat selection, i.e. an habitat selection pattern that depends on habitat availability (Myerud and Ims (1998)); an habitat type can therefore be preferred by a species in a context and avoided in another (e.g. Calenge et al. (2005)). Similarly, our approach supposes that the observers in the citizen science program show a constant preference in space and time. However, the observers preferences can also be characterized by functional responses. For example, in an opportunistic data collection program focusing on birds, observers may be more interested by waterbirds in humid regions and therefore prefer to spend their time close to lakes and ponds in such regions, as this is where they are more likely to observe the species of interest. On the other hand, in a mountainous region, observers might be more interested into raptors and avoid lake and ponds. Such functional response of the observers can bias the resulting estimates, and should be seriously considered when fitting this model.

Possible extension. So far, we assumed that the detectability P_{ik} of species i in dataset k does not depend on the habitat type, which might be unrealistic since, in particular, the range of vision of an observer can be different from one habitat type to the other. If so, our estimation of habitat selection parameters S_{ih} can be biased. Due to identifiability constraints, we cannot include in the model and estimate an unknown list of parameters α_h taking into account the dependence of detectability to habitat (since they will be undistinguishable from the species habitat selection probabilities S_{ih}). However, it is possible to include these parameters in the model and define an informative prior distribution on these detectabilities, if information is available elsewhere. Another solution is to use additional data concerning the detectability associated to each considered habitat. We demonstrate in Appendix A.5.2 how to implement this approach with the dataset used in this paper, by using additional data that give for different kinds of habitats the respective numbers of observations made in different ranges of distances. Based on an idea similar to the statistical approach underlying the abundance estimation based on distance sampling (Buckland et al. (1993)), we demonstrate how to estimate and account for the variable detectability between habitat types when estimating the species relative abundance in each site.

Issues when implementing the model. Several issues must be carefully handled when implementing our model on some datasets. A key step in the implementation of our model lies in the choice of the habitat types and their number. This choice, which is dataset dependent, must be handled with care. First, the choice of the habitat types must be meaningful for the monitored species. For example, assume that some of the monitored species have a very different selection probability for two given habitat types, say "deciduous forest" and "coniferous forest". If the proportion of "deciduous forest" and "coniferous forest" varies from one site to the other, then the merging of these two habitat types into a single habitat type "forest" would induce a significant bias in the estimation. To avoid such biases, we may be tempted to select a very large number of habitat types, ensuring a strong homogeneity of each type. Yet, the multiplication of the habitat types is limited by the number of available observation points in each habitat type. Actually, in order to avoid a detrimental increase of the variance, we need to have enough observation points in each habitat type. These observations can be indifferently in the opportunistic or in the standardized dataset. So, when choosing the habitat types (and their number), one must find a good balance between defining meaningful habitat types for the monitored species and having enough observations in each habitat type. Another major degree of freedom in the implementation of the model, is the choice of the number of species. On the one hand, increasing the number of species helps the estimation, since the ratio between the number of observations and the number of parameters then decreases. On the other hand, including some rare species, or including some species which require to add some new habitat types, can harm the estimation by increasing the variance. So, again, a good balance must be found between the two phenomena.

For a fair comparison of the statistical models with and without habitat modeling, we have implemented our model with very flat priors on all the parameters. In practice, we may have access to some existing estimates for some of the parameters. For example, for some species, we can have some estimates for some of the habitat probabilities of selection (Manly et al. (2002)). In this case, it is worth to incorporate this knowledge by designing some more informative priors on the habitat probabilities of selection.

Acknowledgements: *The authors would like to thank Benjamin Auder for his contribution*

Table 3: List of the 34 bird species under study. The 13 species that are monitored by the ACT survey are indicated by an asterisk.

| Latin name | Species | Latin name | Species |
|--------------------------------|---------------------------|--------------------------------|------------------------|
| <i>Aegithalos caudatus</i> | Long-Tailed Tit | <i>Alauda arvensis</i> * | Eurasian Skylark |
| <i>Alectoris rufa</i> * | Red-Legged Partridge | <i>Carduelis carduelis</i> | European Goldfinch |
| <i>Carduelis chloris</i> | European Greenfinch | <i>Certhia brachydactyla</i> | Short-Toed Treecreeper |
| <i>Columba palumbus</i> * | Common Wood Pigeon | <i>Coturnix coturnix</i> * | Common Quail |
| <i>Cuculus canorus</i> | Common Cuckoo | <i>Cyanistes caeruleus</i> | Eurasian Blue Tit |
| <i>Dendrocopos major</i> | Great Spotted Woodpecker | <i>Erithacus rubecula</i> | European Robin |
| <i>Fringilla coelebs</i> | Common Chaffinch | <i>Garrulus glandarius</i> * | Eurasian Jay |
| <i>Hippolais polyglotta</i> | Melodious Warbler | <i>Lullula arborea</i> * | Woodlark |
| <i>Luscinia megarhynchos</i> | Common Nightingale | <i>Milvus migrans</i> | Black Kite |
| <i>Parus major</i> | Great Tit | <i>Passer domesticus</i> | House Sparrow |
| <i>Phasianus colchicus</i> * | Common Pheasant | <i>Phoenicurus ochruros</i> | Black Redstar |
| <i>Phylloscopus collybita</i> | Common Chiffchaff | <i>Pica pica</i> * | Eurasian Magpie |
| <i>Pica viridis</i> | Eurasian Green Woodpecker | <i>Sitta europaea</i> | Eurasian Nuthatch |
| <i>Streptopelia decaocto</i> * | Eurasian Collared Dove | <i>Streptopelia turtur</i> * | European Turtle Dove |
| <i>Sylvia atricapilla</i> | Eurasian Blackcap | <i>Troglodytes troglodytes</i> | Eurasian Wren |
| <i>Turdus merula</i> * | Common Blackbird | <i>Turdus philomelos</i> * | Song Thrush |
| <i>Turdus viscivorus</i> * | Mistle Thrush | <i>Upupa epops</i> | Eurasian Hoopoe |

to the computer code for data treatment. We sincerely thank Denis Roux and all observers from the ACT network. We also thank the managers of both programs « Faune d'Aquitaine » and STOC-EPS, as well as the observers participating to these programs. This work was partially funded by public grants as part of the "Investissement d'avenir" project, reference ANR-11-LABX-0056-LMH, LabEx LMH, and reference ANR-10-CAMP-0151-02, Fondation Mathématiques Jacques Hadamard, by the Chair "Modélisation Mathématique et Biodiversité" of VEOLIA-Ecole Polytechnique-MNHN-F.X, and by the Mission for Interdisciplinarity at CNRS.

A Appendix

A.1 List of species

Table 3 provides the list of the 34 bird species under study.

A.2 Identifiability and models implementation

A.2.1 Reparametrization of the model

Let us recall our model for the observations, where c is a cell of the site j :

$$\begin{aligned} X_{ick} &\sim \text{Poisson} \left(\int_{\mathcal{A}_c} N_{ij} \frac{S_{ih(x)}}{\sum_{h'} S_{ih'} V_{h'j}} \times E_{ck} \frac{q_{h(x)k}}{\sum_{h'} q_{h'k} V_{h'c}} \times P_{ik} dx \right) \\ &= \text{Poisson} \left(N_{ij} E_{ck} P_{ik} \sum_h \frac{q_{hk}}{\sum_{h'} q_{h'k} V_{h'c}} \frac{S_{ih}}{\sum_{h'} S_{ih'} V_{h'j}} V_{hc} \right). \end{aligned}$$

For standardized data, we can assume either that q_{h0}/q_{10} is known for all h (generally equal to 1), or that each cell for the standardized dataset is small enough to be composed with only one habitat. In addition, we assume that E_{c0}/E_{10} is known for all c for the standardized dataset. To implement our model while ensuring identifiability of the parameters, we use the following change of variables

$$\tilde{N}_{ij} = \frac{N_{ij} P_{i0} E_{10}}{\sum_{h'} \frac{S_{ih'}}{S_{i1}} V_{h'j}}, \quad \tilde{P}_{ik} = \frac{P_{ik} P_{10}}{P_{i0} P_{1k}}, \quad \tilde{E}_{ck} = \frac{E_{ck} P_{1k}}{P_{10} E_{10}} \frac{V_c}{\sum_{h'} \frac{q_{h'k}}{q_{1k}} V_{h'c}},$$

$$\tilde{q}_{hk} = \frac{q_{hk}}{q_{1k}}, \quad \tilde{S}_{ih} = \frac{S_{ih}}{S_{i1}}$$

where $V_c = \sum_h V_{hc}$. Using this change of variables, we get that for all i, c and k ,

$$X_{ick} \sim \mathcal{P} \left(\tilde{N}_{ij} \tilde{E}_{ck} \tilde{P}_{ik} \sum_h \tilde{q}_{hk} \tilde{S}_{ih} V_{hc} \right)$$

with

$$\frac{\tilde{N}_{ij}}{\tilde{N}_{i1}} = \frac{N_{ij} \sum_{h'} \tilde{S}_{ih'} V_{h'1}}{N_{i1} \sum_{h'} \tilde{S}_{ih'} V_{h'j}}, \quad \tilde{P}_{i0} = 1, \quad \tilde{P}_{11} = 1, \quad \tilde{q}_{h0} = 1, \quad \tilde{q}_{11} = 1, \quad \tilde{S}_{i1} = 1$$

for all i, c, k , and \tilde{E}_{c0} is known for all c .

In particular for standardized data, for which we can assume that the habitat associated to each cell c is known (denoted by $h(c)$), we get:

$$X_{ic0} \sim \mathcal{P} \left(\tilde{N}_{ij} \tilde{E}_{c0} \tilde{S}_{ih(c)} \right),$$

where \tilde{E}_{c0} is known for all cell c . This is a generalized linear model with $IJ + I(H - 1)$ unknown parameters (the quantities \tilde{N}_{ij} as well as habitat selection parameters \tilde{S}_{ih}/S_{i1} for $h > 1$). These parameters are identifiable if and only if the matrix Y with size $C \times (J + H - 1)$ giving for each cell c visited by the STOC dataset, the site and habitat associated to this cell (when this habitat is not the first habitat), has rank $J + H - 1$. More precisely, the matrix Y is such that for all $c \in \llbracket 1, C \rrbracket$, $Y_{cj(c)} = 1$, $Y_{cJ+(h(c)-1)} = 1$ if $h(c) > 1$, and $Y_{cl} = 0$ elsewhere.

A.2.2 Implementation with JAGS

The computer code associated to the section 3.1 is given in the numerical Additional File SimulatedData.Rnw. This program calls three models that are written in separate files: one for our model (Additional file ModelSimulatedData.txt), one for the model in which we use only standardized data (Additional file ModelStandardizedSimulatedData.txt), and one for the model in which differences in habitat preferences are neglected (Additional file ModelWithoutHabitatSimulatedData.txt).

The computer code associated to the section 2 is given in the numerical Additional File RealData.Rnw. This program calls four models that are written in separate files: one for our model (Additional file ModelWithHabitat.txt), one for the model in which we use only standardized data (Additional file ModelStandardizedOnly.txt), one for the model in which differences in habitat preferences are neglected (Additional file ModelWithoutHabitat.txt), and one for the model in space is considered as one single quadrat (Additional file ModelOneQuadrat.txt).

A.3 Some details on the numerics: the prediction of the STOC data

Let \mathcal{C}_j^{STOC} denote the set of all the observation points c in the quadrat j surveyed in the STOC dataset. The STOC counts for the species i in the quadrat j are

$$X_{ij}^{STOC} = \sum_{c \in \mathcal{C}_j^{STOC}} X_{ic}^{STOC}.$$

Let us denote by $h(c)$ the habitat type of the observation point c . In our model (2), the average number of individuals of the species i in the square $c \in \mathcal{C}_j^{STOC}$ is given by

$$\int_{\mathcal{A}_c} \frac{N_{ij} S_{ih(c)}}{\sum_{h'} S_{ih'} V_{h'j}} dx = \frac{N_{ij} S_{ih(c)} V_c}{\sum_{h'} S_{ih'} V_{h'j}}.$$

Taking into account a variable observational effort E_c^{STOC} on each observation point c , we then predict X_{ij}^{STOC} from the estimation based on our Model (2) by

$$\hat{X}_{ij}^{model} = \hat{N}_{ij}^{model} \sum_{c \in \mathcal{C}_j^{STOC}} E_c^{STOC} \frac{\hat{S}_{ih(c)}^{model} V_c}{\sum_{h'} \hat{S}_{ih'}^{model} V_{h'j}},$$

where the observational effort E_c^{STOC} is given by the number of years of observation at the observation point c .

For the one quadrat model with habitat [One Quadrat with hab] displayed in Table 2, the prediction is given by

$$\hat{X}_{ij}^{model} = \hat{N}_i^{model} \sum_{c \in \mathcal{C}_j^{STOC}} E_c^{STOC} \frac{\hat{S}_{ih(c)}^{model} V_c}{\sum_{h'} \hat{S}_{ih'}^{model} V_{h'}},$$

with $V_{h'}$ the area of the habitat type h' in the whole quadrat.

When the Model (1) is used for estimation, then the predictions are given by

$$\hat{X}_{ij}^{model} = \hat{N}_{ij} \sum_{c \in \mathcal{C}_j^{STOC}} E_c^{STOC} \frac{V_c}{V_j}.$$

A.4 Additional results on simulated data

In this section we provide additional results to the ones presented in Section 3.1 for simulated data. Figure 5, as a complement to Figure 1, provides the posterior distributions of the habitat selection probabilities S_{i2} for all i , showing that these posterior are a good approximations to the reference values that we wish to estimate. Figure ??, as a complement to Figure 1 gives the boxplots of the mean of the squared difference between the posterior distribution and the real value of relative abundances, for the different considered models and datasets.

A.5 Additional results on real data

A.5.1 Some ecological results

In this section we provide additional results with ecological motivations.

In Figure 6 we give a map of the estimated densities of the Grimpereau, with and without habitat structure. In Figure 7 we give the mean preferences of all considered species, for each habitat type.

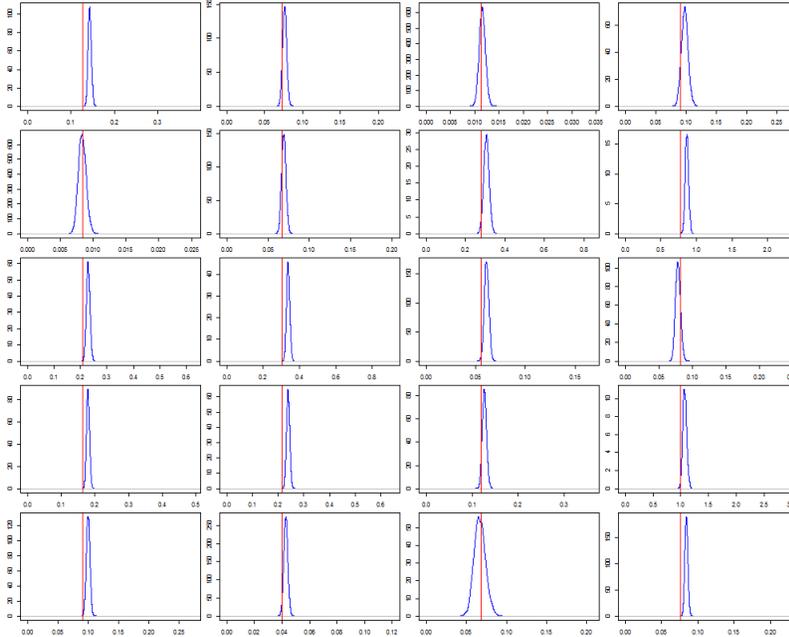


Figure 5: Posterior distributions of the habitat selection probabilities S_{i2} for all i ($S_{i1} = 1$ for all i , each graph corresponds to a different value of i). The reference values are given in red.

A.5.2 Taking into account habitat dependent detectability

We so far assumed that the detectability P_{ik} of species i in dataset k does not depend on the habitat, which might be unrealistic since, in particular, the range of vision (or hearing) can be different from one habitat to the other. If so, our estimation of habitat selection parameters S_{ih} but also of species relative abundances can be biased. Due to identifiability constraints, we cannot add and estimate an unknown list of parameters α_h taking into account the dependence of detectability to habitat (since they will be undistinguishable from the species habitat selection probabilities S_{ih}). Our proposition is to use an auxiliary dataset that can provide informations concerning the detectability associated to each considered habitat. We test this idea using a dataset provided by VigieNature that gives for different kinds of habitats the respective numbers of observations made in different ranges of distance. The program associated to this section is given in the file alpha.R.

For each habitat h , we can assume that detection probability is equal to 1 when observed individuals are "close enough" to the observer, since we only want to quantify the loss in detectability in each habitat due to the limitation in range of vision (or hearing) in this habitat. More precisely, we assume that detection probability is equal to 1 when the observed individual is less than 25 meters far from the observer. Then if we denote by Y_h the number of observed individuals in habitat h and by Y_{1h} the number of observed individuals in habitat h , at distance less than 25 meters from the observer, we can quantify the detectability in habitat h by the quantity

$$\alpha_h = \frac{Y_h/Y_{1h}}{Y_1/Y_{11}}.$$

The result of these calculations is given in Table 4. As expected, the detectability is lower

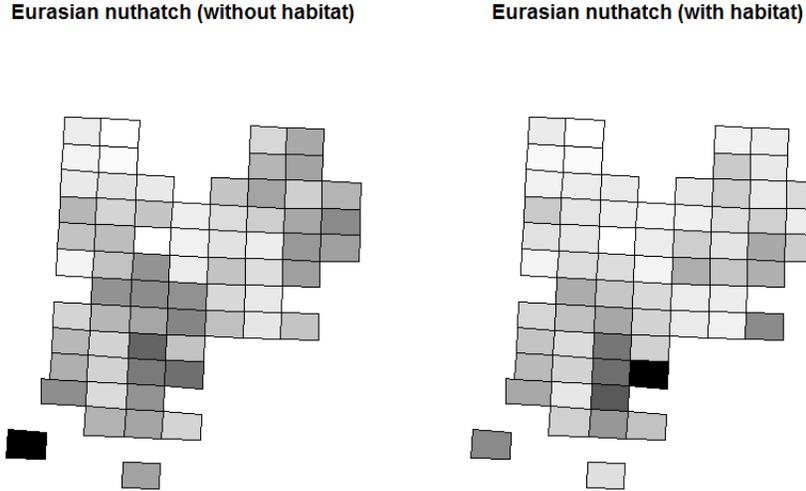


Figure 6: Relative density maps of the European nuthatch, without (left), and with (right) taking into account habitat structure. For each quadrat the gray level indicates the relative density $\frac{\hat{N}_{ij}^{model} V_l}{\hat{N}_{i1}^{model} V_j}$ where V_l is the area of quadrat l .

in urbanized area and forest than in open and agricultural landscapes. The impact of taking into account habitat detectability is illustrated in Figure 7.

| Corine land Cover Habitat | Detectability α_h |
|--------------------------------------|--------------------------|
| Urbanized area | 1 |
| Intensive agriculture | 1.72 |
| Open natural landscape | 1.71 |
| Farmland with heterogenous landscape | 1.72 |
| Mixed forest | 1.47 |
| Deciduous forest | 1.47 |
| Coniferous forest | 1.47 |

Table 4: The detectability associated to each habitat, taking account differences in ranges of vision.

References

Bellamy, P. E., N. J. Brown, B. Enoksson, L. G. Firbank, R. J. Fuller, S. A. Hinsley, and A. G. M. Schotman (1998). The influences of habitat, landscape structure and climate on local distribution patterns of the nuthatch (*sitta europaea* l.). *Oecologia* 115(1-2), 127–136.

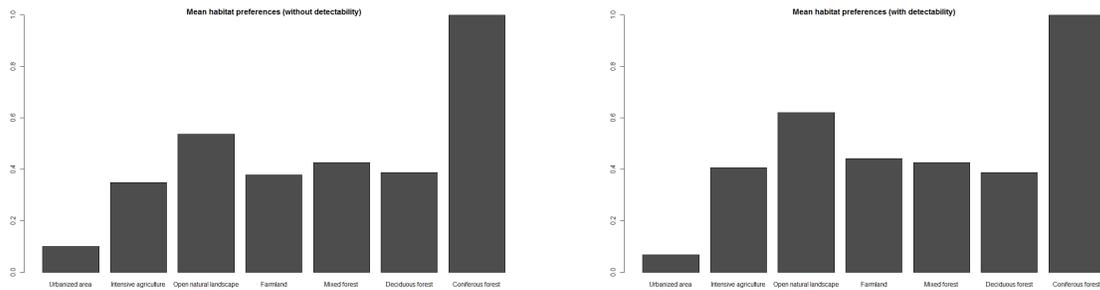


Figure 7: Mean species estimated habitat selection probabilities, without (left) and with (right) habitat dependent detectability.

Biggs, C. R. and J. D. Olden (2011). Multi-scale habitat occupancy of invasive lionfish (pterois volitans) in coral reef environments of roatan, honduras. *Aquatic Invasions* 6, 347–353.

Boutin, J., D. Roux, and C. Eraud (2003). Breeding bird monitoring in france: the act survey. *Ornis Hungarica* 12(13), 1–2.

Boyce, M. and L. McDonald (1999). Relating populations to habitats using resource selection functions. *Trends in Ecology & Evolution* 14, 268–272.

Buckland, S., D. Anderson, K. Burnham, and J. Laake (1993). *Distance Sampling: Estimating Abundance of Biological Populations*. Chapman & Hall, New York.

Calenge, C., A. Dufour, and D. Maillard (2005). K-select analysis: a new method to analyse habitat selection in radio-tracking studies. *Ecological Modelling* 186, 143–153.

Dickinson, J. L., B. Zuckerberg, and D. N. Bontar (2010). Citizen science as an ecological research tool: Challenges and benefits. *Annual Review of Ecology, Evolution, and Systematics* 41(1), 149–172.

Fithian, W., J. Elith, T. Hastie, and D. Keith (2014). Bias correction in species distribution models: Pooling survey and collection data for multiple species. *to appear in Methods for Ecology and Evolution*.

Fuller, R. M., B. J. Devereux, S. Gillings, G. S. Amable, and R. A. Hill (2005). Indices of bird-habitat preference from field surveys of birds and remote sensing of land cover: a study of south-eastern england with wider implications for conservation and biodiversity assessment. *Global Ecol. Biogeogr.* 14, 223–239.

Giraud, C., C. Calenge, C. Coron, and R. Julliard (2015). Capitalizing on opportunistic data for monitoring species relative abundances. *Biometrics* 72(2), 649–58.

Isaac, N. J. B., A. J. van Strien, T. A. August, M. P. de Zeeuw, and D. B. Roy (2014). Statistics for citizen science: extracting signals of change from noisy ecological data. *Methods in Ecology and Evolution*.

Jiguet, F., V. Devictor, R. Julliard, and D. Couvet (2012). French citizens monitoring ordinary birds provide tools for conservation and ecological sciences. *Acta Oecologica* 44, 58 – 66.

- Lele, S. R., E. H. Merrill, J. Keim, and M. S. Boyce (2013). Selection, use, choice and occupancy: clarifying concepts in resource selection studies. *Journal of Animal Ecology* 82, 1183–1191.
- Link, W. A. and J. R. Sauer (1998). Estimating population change from count data: application to the north american breeding bird survey. *Ecological Applications* 8, 258–268.
- MacKenzie, D. (2005). What are the issues with presence–absence data for wildlife managers? *Journal of Wildlife Management* 69, 849–860.
- Mair, L. and A. Ruede (2016). Explaining spatial variation in the recording effort of citizen science data across multiple taxa. *PLOS ONE* 11(1), 1–13.
- Manly, B., L. McDonald, D. Thomas, T. MacDonald, and W. Erickson (2002). *Resource selection by animals. Statistical design and analysis for field studies*. London: Kluwer Academic Publisher.
- Mason, C. F. and S. M. Macdonald (2004). Distribution of foraging rooks, *corvus frugilegus*, and rookeries in a landscape in eastern england dominated by winter cereals. *Folia Zool.* 53(2), 179–188.
- Mysterud, A. and R. Ims (1998). Functional responses in habitat use: availability influences relative use in trade-off situations. *Ecology* 79, 1435–1441.
- Phillips, S., M. Dudík, J. Elith, C. Graham, A. Lehmann, J. Leathwick, and S. Ferrier (2009). Sample selection bias and presence-only distribution models: implications for background and pseudo-absence data. *Ecological Applications* 19, 181–197.
- Plummer, M. (2003). Jags: A program for analysis of bayesian graphical models using gibbs sampling.
- Plummer, M. (2014). *rjags: Bayesian graphical models using MCMC*. R package version 3-13.
- Pollock, K. H. (1982). A capture recapture design robust to unequal probability of capture. *J. Wildlife Management* 46, 752–757.
- R Core Team (2014). *R: A Language and Environment for Statistical Computing*. Vienna, Austria: R Foundation for Statistical Computing.
- Royle, J. A., J. D. Nichols, and M. Kéry (2005). Modelling occurrence and abundance of species when detection is imperfect. *Oikos* 110(2), 353–359.
- Tulloch, A. and J. Szabo (2012). A behavioural ecology approach to understand volunteer surveying for citizen science datasets. *Emu* 112, 313–325.