



Groupe de travail « Schémas de Boltzmann sur réseau » — 24 février 2021.

LBM – reactive flows

P. Boivin (et al. surtout)



Outline

- * Part I : M2P2 & me...
- * Part II : LBM : price & prejudices
- * Part III : LBM & reactive flows (theory)
- * Part IV : Validations (academic & benchmarks)
- * Part V: Towards complex configurations
- * Part VI : Discussion, perspectives





- ★ ~40 EC+C (permanent staff)
- * 3 tutelles, 2 sites: Ecole Centrale Marseille & Arbois
- * Membre Fédération Fabri de Peiresc (IRPHE, IUSTI, LMA)
- * Membre de l'Institut de Mécanique et d'Ingénierie (Idex Marseille)
- 6 équipes de recherches en mécanique et génie des procédés
- * TONIC: Thermodynamique, Ondes, Numérique, Instabilités, Combustion. 7 permanents, 2 émérites.
- * Financement industriel ~ 80%.

M2P2

About me...



Since 201

2014-2016

2012-2013

2009-2011

2007-2008

2006-2007

2003-2007

6 : CNRS research fellow	 * TONIC team lead * CR @ M2P2
6: Post-doctoral studies	 CNES + ANR UC3M
3: Snecma (Vernon)	 Cryogenic engine Ignition specialis
l: PhD - UC3M (Madrid)	* PhD cum laude
8: PSA (Vélizy)	* MSc thesis
7: KTH (Stockholm)	 Double degree
7: Ecole Polytechnique	 Diplôme d'ingén







Main research lines

- Difficulty in developing methods able to encompass both multiphase (including a dense part) and reactive flows
 - * Multiphase & reactive flows have evolved in separate disciplines
 - * Development of thermodynamics & kinetics model simple enough for use in practical applications





Coaxial flame (cryogenic injector)



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A short & naive history of LBM

- * Hard to work on real geometries: meshing can take up to 3 weeks.
- * Coding and scaling NS codes is tedious
- * Powerflow came up ~2007 at PSA, doing « free » computations
- * Now (2015!) claims to have 85% market share on car aerodynamics
- and co-developed at M2P2

Assessment of DES/DDES for external aerodynamics

- Experiments @S2A windtunnel
- * Numerics @Ansys France





* Expensive > ProLB, French consortium including AMU, Renault, Airbus...





LBM - principles







LBM - principles

Lattice Boltzmann equation





But...

$p = \rho \cdot c_s^2$

Classical (athermal) LBM only solves mass & momentum equations...

Some prejudices about LBM for combustion

- * LBM is for rarefied gases and the Chapman Enskog expansion is dubious, so why bother ?
- Extending LBM to multicomponent requires many distributions
 can become stringent in terms of memory usage
- * The expensive part of a NS solver is computing combustion related quantities (diffusion / kinetics / ...).
- * From the last point, one could infer that the same could be obtained with an octree cartesian NS solver.

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Combustion - macroscopic equations

	Thermod
Macroscopic equations	$\rho = \rho \overline{r} T$
$\frac{\partial \rho}{\partial t} + \frac{\partial \rho u_{\beta}}{\partial x_{\beta}} = 0$	$\overline{F} = R/\overline{W}$
$\frac{\partial \rho u_{\alpha}}{\partial t} + \frac{\partial \rho u_{\alpha} u_{\beta} + p \delta_{\alpha\beta} - \mathcal{T}_{\alpha\beta}}{\partial x_{\beta}} = 0$	$=\sum_{k=1}^{N}h_{k}Y_{k}, h_{k}$
$\rho \frac{\partial h}{\partial t} + \rho u_{\alpha} \frac{\partial h}{\partial x_{\alpha}} = \frac{Dp}{Dt} - \frac{\partial q_{\alpha}}{\partial x_{\alpha}} + \mathcal{T}_{\alpha\beta} \frac{\partial u_{\alpha}}{\partial x_{\beta}}$ $\rho \frac{\partial Y_{k}}{\partial t} + \rho u_{\alpha} \frac{\partial Y_{k}}{\partial x_{\alpha}} = \frac{\partial}{\partial x_{\alpha}} (-\rho Y_{k} V_{k,\alpha}) + \dot{\omega}_{k}$	$\begin{aligned} & D \\ V_{k,\alpha} = -D_k \frac{\partial X_k}{\partial x_\alpha} \\ V_{\alpha}^c = \sum_{k=1}^N D_k \frac{\partial X_k}{\partial x_\alpha} \end{aligned}$

lynamic closure

$$\overline{W} = \frac{1}{\sum_{k} Y_{k} / W_{k}}$$

$$= \int_{T_0} C_{p,k}(T) dT + \Delta h_{f,k}^0$$

Viscous term

$$\mathcal{T}_{\alpha\beta} = \rho\nu \left(\frac{\partial u_{\alpha}}{\partial x_{\beta}} + \frac{\partial u_{\beta}}{\partial x_{\alpha}} - \delta_{\alpha\beta} \frac{2}{3} \right)$$

$$\mu = \mu_0 \left(\frac{T}{T_0} \right)^{\beta}$$

Diffusion terms

$$\frac{W_{k}}{\overline{W}} + V_{\alpha}^{c}Y_{k} \qquad D_{k} = \frac{\mu}{\rho Sc_{k}}$$

$$\frac{W_{k}}{\overline{W}} \qquad \lambda = \frac{\mu}{\Pr} \sum_{k=1}^{N} Y_{k}C_{p,k}$$

$$= -\lambda \frac{\partial T}{\partial x_{\alpha}} + \rho \sum_{k=1}^{N} h_{k}Y_{k}V_{k,\alpha}$$

Fully defined provided EOS given (Nasa polynomials) Sc_k provided for each species Pr provided - $\mu(T)$ law given - $\dot{\omega}_k$ given via kinetic scheme







LBM – M

$$\frac{\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho u) = 0}{\frac{\partial \rho u}{\partial t} + \nabla \cdot (\rho u u) = -\nabla p + \nabla \cdot [\rho \nu (\nabla u + (\nabla u)^T)]}$$

$$+$$

$$\frac{\partial T}{\partial t} + u_{\alpha} \frac{\partial}{\partial x_{\alpha}} T = \frac{1}{\rho} \frac{\partial}{\partial x_{\alpha}} (\rho D_T \frac{\partial T}{\partial x_{\alpha}}) + \frac{\omega_h}{\rho c_p}$$

$$+$$

$$\frac{\partial Y_k}{\partial t} + u_{\alpha} \frac{\partial}{\partial x_{\alpha}} Y_k = \frac{1}{\rho} \frac{\partial}{\partial x_{\alpha}} (\rho D_k \frac{\partial Y_k}{\partial x_{\alpha}}) + \frac{\omega_k}{\rho}$$

Possible Strategies



Hybrid LBM (v1: density - based)

- * Mass conservation
- * Momentum conservation
- $\begin{aligned} \frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \boldsymbol{u}) &= 0\\ \frac{\partial \rho \boldsymbol{u}}{\partial t} + \nabla \cdot (\rho \boldsymbol{u} \boldsymbol{u}) &= -\nabla p + \nabla \cdot \begin{vmatrix} \mathbf{u} \\ \mathbf{v} \end{vmatrix} \\ f_i(\boldsymbol{x} + \boldsymbol{c} \delta t, t + \delta t) f_i(\boldsymbol{x}, t) &= -\mathbf{v} \\ f_i^{eq} &= \rho w_i \left[1 + \frac{\boldsymbol{c}_i \cdot \boldsymbol{u}}{c_s^2} + \mathbf{v} \right] \\ + (\theta 1) \left(\frac{1}{2} (\frac{\boldsymbol{c}_i^2}{c_s^2} D) + \frac{\boldsymbol{c}_i \cdot \boldsymbol{u}}{2c_s^2} \right) \end{aligned}$

$$\theta = \frac{\overline{r}T}{c_s^2} = \frac{RT}{c_s^2} \sum_k \frac{Y_k}{W_k} = f(T, Y_k)$$

$$\frac{\partial T}{\partial t} + u_{\alpha} \frac{\partial}{\partial x_{\alpha}} T = \frac{1}{\rho} \frac{\partial}{\partial x_{\alpha}} (\rho D_T \frac{\partial T}{\partial x_{\alpha}}) + \frac{\omega_h}{\rho c_p}$$
$$\frac{\partial Y_k}{\partial t} + u_{\alpha} \frac{\partial}{\partial x_{\alpha}} Y_k = \frac{1}{\rho} \frac{\partial}{\partial x_{\alpha}} (\rho D_k \frac{\partial Y_k}{\partial x_{\alpha}}) + \frac{\omega_k}{\rho}$$

- * Energy conservation
- * Species conservation

$$\cdot \left[\rho \nu (\nabla \boldsymbol{u} + (\nabla \boldsymbol{u})^T) \right]$$

Chapman-Enskog or Taylor Expansion

$$-\frac{1}{\tau}[f_{i}(\boldsymbol{x},t) - f_{i}^{eq}(\boldsymbol{x},t)] + \frac{(\boldsymbol{c}_{i} \cdot \boldsymbol{u})^{2}}{2c_{s}^{4}} - \frac{\boldsymbol{u}^{2}}{2c_{s}^{2}} - \frac{\boldsymbol{u}^{2}}{2c_{s}^{2}} - \frac{\boldsymbol{u}^{2}}{2c_{s}^{2}} + \frac{\boldsymbol{u}^{2}}{2c_{s}^{2}} + \frac{\boldsymbol{u}^{2}}{2c_{s}^{2}} - \frac{\boldsymbol{u}^{$$



Successes with v1: premixed flame.



Chemistry: One Step - Propane (S. Chen et al. (2007), AMC)

 C_3H_8 -air - 1s Lewis transp. Cp(T)



Diffusion flame

Fuel inlet



Oxidizer inlet





Going more complex...



Fig. 6. Doubly periodic shear layer at $Re = 3.10^4$. Vorticity contours (magnitude of the z-component) at $t = t_c$. NTMIX contours (left) compared with the LBM contours (right), for the compressible "cold" flow (top) and the "hot" flow (bottom), e.g. including the chemical source term, on a 1024×1024 grid.



top to bottom: case A at t = 2.12 and t = 2.83; case B at t = 1.42 and t = 1.80; case C at t = 0.90 t = 1.09.

... and quickly reaching limitations ...



Vortex/flame (hydrogen, 12 steps)



« Spherical flame »

General idea for model 2.0

- * About segregated density/pressure-based methods
 - * A classical CFD approach (1980s now) for "all speed methods"
 - * used in FLUENT, STARCCM+, some OpenFoam versions ...
- * Generic structure
 - * Predictor step (starting from (u^n, p^n, T^n, ρ^n))
 - compute intermediary variables (*u**, *p**, *T**, *ρ**) s
 implicit) method
 - * Segregated = energy equation solved separately from mass+momentum
 - * Corrector step
 - * Solve an equation for pressure/density correction to recover full compressibility
 - * update other variables using the new pressure/density $(u^*, p^*, T^*, \rho^*) \rightarrow (u^{n+1}, p^{n+1}, T^{n+1}, \rho^{n+1})$

* compute intermediary variables (u^* , p^* , T^* , ρ^*) solving a (nearly) incompressible problem with a robust (usually

Model 1.0 « density »

- * Resolution for f
- * $(\theta 1)$ term in f_{ea}
- 3rd order eq. Distribution •

$$\begin{cases} \sum_{i} f_{i} = \rho \\ \sum_{i} c_{i,\alpha} f_{i} = \rho u_{\alpha} \\ \sum_{i} c_{i,\alpha} c_{i,\beta} f_{i} = \rho u_{\alpha} u_{\beta} + \rho c_{s}^{2} \delta_{\alpha\beta} \end{cases}$$

- Collision kernel: hybrid regularized ($\sigma \in [0,0.5]$)
- * Correction term to account for the lattice defect (stress tensor)

[1] Y. Feng, M. Tayyab, and P. Boivin, "A lattice-boltzmann model for low-mach reactive flows," Combustion and Flame, vol. 196, pp. 249 – 254, 2018.

[2] Y. Feng, P. Boivin, J. Jacob, and P. Sagaut, "Hybrid recursive regularized thermal lattice boltzmann model for high subsonic compressible flows," Journal of Computational Physics, vol. 394, pp. 82 – 99, 2019.

Model 2.0 « pressure »

- * Resolution for g
- * Athermal formulation for g_{eq} (orders > 0)
- * 2nd order is enough...

$$\begin{cases} \sum_{i} g_{i} = \rho \theta \\ \sum_{i} c_{i,\alpha} g_{i} = \rho u_{\alpha} \\ \sum_{i} c_{i,\alpha} c_{i,\beta} g_{i} = \rho u_{\alpha} u_{\beta} + \rho \theta c_{s}^{2} \delta_{\alpha\beta} \end{cases}$$

- * Modified macroscopic variable reconstruction $\rho(t + \Delta t, x) = \sum \left[g_i^*(t + \Delta t, x) \right] - \rho(t, x) \theta(t, x) + \rho(t, x)$
- * Additional 2nd order correction needed $a_{\alpha\beta}^{\rm cor} \equiv c_s^2 \delta_{\alpha\beta} \left[\rho(t + \Delta t, x)(1 - \theta(t + \Delta t, x)) - \rho(t, x)(1 - \theta(t, x)) \right]$

[1] G. Farag, S. Zhao, T. Coratger, P. Boivin, G. Chiavassa, and P. Sagaut, "A pressure-based regularized lattice-boltzmann method for the simulation of compressible flows," Physics of Fluids, vol. 32, no. 6, p. 066106, 2020.





Pressure-based vs Density-based



 H_2 -air - 12s Lewis transp. Cp(T)



⁽b) t= 4.0×10^{-2} ms

References

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- * Y. Feng, P. Boivin, J. Jacob, and P. Sagaut, "Hybrid recursive regularized thermal lattice boltzmann model for high subsonic compressible flows," Journal of Computational Physics, vol. 394, pp. 82 – 99, 2019. (v1)
- * M. Tayyab, S. Zhao, Y. Feng, and P. Boivin, "Hybrid regularized lattice-boltzmann modelling of premixed and non-premixed combustion processes," Combustion and Flame, vol. 211, pp. 173–184, 2020. (v1)
- * G. Farag, S. Zhao, T. Coratger, P. Boivin, G. Chiavassa, and P. Sagaut, "A pressure-based regularized lattice-boltzmann method for the simulation of compressible flows," Physics of Fluids, vol. 32, no. 6, p. 066106, 2020. (v2)
- * M. Tayyab, B. Radisson, C. Almarcha, B. Denet, and P. Boivin, "Experimental and numerical lattice-boltzmann investigation of the darrieuslandau instability," Combustion and Flame, vol. 221, pp. 103–109, 2020. (v2)
- * S. Zhao, G. Farag, P. Boivin, and P. Sagaut, "Toward fully conservative hybrid lattice boltzmann methods for compressible flows," Physics of Fluids, vol. 32, no. 12, p. 126118, 2020. (v2)
- * M. Tayyab, S. Zhao, and P. Boivin, "Lattice-boltzmann modelling of a turbulent bluff-body stabilized flame," Physics of Fluids, 2021. (v2) * G. Farag, S. Zhao, G. Chiavassa, and P. Boivin, "Consistency study of lattice-boltzmann schemes macroscopic limit," Physics of Fluids, 2021.
- (Theory)





Remarks

- periodic domains
- * A priori compatible with your favorite collision kernel...

* Mass is (non-trivially) globally conserved as before for closed

And the scalar equations ?

- * Scalar equations are solved on the same grid.
- Explicit time-stepping is used (same time-step as LB time-step) yet, the method is 2nd order in time •
- * Finite volume methods to compute all RHS terms
 - * Second-order isotropic operator = non-conservative form (OK for Ma<0,3)
 - * Or MUSCL = non-conservative form (necessary for higher speeds)
 - * Or (new) flux reconstruction from LB mass fluxes = conservative form
 - Coupling is paramount...
- * Any number of explicit advection / diffusion equation

can be included (energy / mass fraction / liquid / spray/...)



Compressible core



Chaire ALBUMS



Entropy equation (MUSCL)





Conserving Scalars...

- * For any advection equation $\frac{\partial \rho \phi}{\partial t} + \nabla \rho u \phi = 0$,
 - * (= mass conservation + non-conservative scalar eq)

$$\nabla^{C} \cdot (\rho \boldsymbol{u} \boldsymbol{\phi}) \equiv \frac{1}{\Delta t} \sum_{i} \left[f_{i}^{\text{col}} \frac{\boldsymbol{\phi}^{+} + \boldsymbol{\phi}}{2} - f_{i}^{\text{col}^{-}} \frac{\boldsymbol{\phi} + \boldsymbol{\phi}}{2} \right]$$

- * ~ Match the LBM mass flux computation to compute scalar eqs.
- * => numerically conserve $\rho\phi$ and $\rho\phi^2$
- * And respect the Hugoniot jump conditions !
- S. Zhao, G. Farag, P. Boivin, and P. Sagaut, "Toward fully conserva 32, no. 12, p. 126118, 2020.



S. Zhao, G. Farag, P. Boivin, and P. Sagaut, "Toward fully conservative hybrid lattice boltzmann methods for compressible flows," Physics of Fluids, vol.

Conserving Scalars...



2D Riemann problem. Conservative form is mandatory to properly capture Hugoniot jumps...

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$1: H + O_2 \rightleftharpoons OH + O$	$7: HO_2 + OH \rightarrow H_2O + O$
$2: H_2 + O \rightleftharpoons OH + H$	$8: H + OH + M \rightleftharpoons H_2O$ -
$3: H_2 + OH \rightleftharpoons H_2O + H$	$9:2\ H+M \rightleftharpoons H_2+M$
$4: H + O_2 + M \to HO_2 + M$	$10:2\ HO_2\to H_2O_2+O_2$
$5: HO_2 + H \to 2 OH$	$11: HO_2 + H_2 \to H_2O_2 +$
$6: HO_2 + H \rightleftharpoons H_2 + O_2$	$12: H_2O_2 + M \to 2 OH +$
Pr: 0.75	$Sc_{O}: 0.53$
$Sc_{H_2}: 0.21$	$Sc_{H_2O}: 0.60$
$Sc_{H}: 0.14$	$Sc_{HO_2} : 0.80$
$Sc_{O_2}: 0.80$	$Sc_{H2O_2} : 0.82$
$Sc_{OH} : 0.53$	$Sc_{N_2}: 1.00$

 $C_p(T) = R(a_1 + a_2T + a_3T^2 + a_4T^3 + a_5T^4)$

$$\mu = \mu_0 \left(\frac{T}{T_0}\right)^{\beta}$$



Spherical premixed flame

- * Isotropy & stability test
- * ~3 pts in flame thickness
- Excellent isotropy

 C_3H_8 -air - 1s Lewis transp. Cp(T)





Spherical premixed flame

- * Isotropy & stability test
- * ~3 pts in flame thickness
- Excellent isotropy
- * Non-reflecting outlets OK

 C_3H_8 -air - 1s Lewis transp. Cp(T)









Vortex-Flame interaction



	V_m/s_L	σ/δ_L	Ka	
Case A	2.24	1.18	1.89	
Case B	16.18	0.93	17.39	
Case C	32.68	0.92	35.52	

Case C: Strong

 H_2 -air - 12s Lewis transp. Cp(T)





























ProLB





 H_2 -air - 12s Lewis transp. Cp(T)









3D Taylor-Green Vortex



- Benchmark DNS for reactive flow
 - * Grids: 256³, 384³, 512³ (mesocentre)
 - ~10 codes participated (ICNC 2019)
- * Comparisons are very good
- * LBM is very (very) fast!

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Combustion instabilities

 $1600.10^{-4}m$ $C_{3}H_{8}, \ \varphi = 0.8$ ^{4}m 2000.10Thermo-diffusive instabilities (propane/air) $\operatorname{Exp}\widetilde{\mathrm{e}}$ Hele-Shaw cell •



Mesh transitions





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3D turbulent jet

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2.1

- Propane non-premixed jet flow (variable density) - Sandia
- 300x200x200 + refinement





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3D turbulent jet

- Propane non-premixed jet flow (variable density) - Sandia
- * 300x200x200 + refinement
- * The same, reactive
 - * No subgrid model (flow)
 - no subgrid model (combustion)
 - * = Highly robust !
- Future work rerun on an experimental jet using a turbulent combustion model





- Common to validate premixed turbulent combustion model
- * Flame stabilized behind bluff body
- Numerical set-up
 - * Min grid size: 2mm, 1mm
 - * 2 step propane chemistry
 - * TFLES model (Rochette C&F 2020)





Velocity field



Progress variable







Cold case













Hot case









Cost: 1000 cpu.h per flow-through-time (5.5M points)



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Conclusions

- * A Hybrid LB model suitable for combustion application
- * Acoustic solver for less the cost of a LMNA code (on uniform grid)
- * Local time-stepping (multi-level grid) => <u>even cheaper</u>
- * Keeps the low-dissipative LB features (aeroacoustics)

Merci à...

- * Muhammad Tayyab (PhD 2017-2020 LBM combustion)
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- * Ceux que j'oublie...

... Questions ?